

• The variation in temperature on the steel nail gives rise to tempering colors.

Dauby et al, LTV Steel, 1985; SM-Cho et al, TMS, 2011 [1]

Flow measurements in the caster





Objectives

- Develop a FLUENT model to simulate the dipping of a nail in the mold of the continuous casting process.
- Verify the accuracy of the model by comparing with the experimental results. Specifically: use tempering colors of steel scale observed on the nails.
- Simulate for steel, aluminum and copper nails.
- Predict a suitable methodology to predict the liquid flux layer thickness using the nail board experiment.







Calculating effective powder thermal conductivities: Equations

• The effective powder thermal conductivity is calculated using the following equation:

$$k_{eff} = \left(\left(\frac{1 - g^{\frac{1}{3}}}{k_{sol}} \right) + \left(\frac{g^{\frac{1}{3}}}{\left(1 - g^{\frac{2}{3}}\right)k_{sol} + g^{\frac{2}{3}}k_{gas}} \right) \right)^{-1}$$

- k_{eff} is the effective powder thermal conductivity
- *k*_{sol} is the solid slag thermal conductivity
- k_{gas} is the thermal conductivity of the gas (Air)
- g is the volume fraction of gas
- The volume fraction of the gas is calculated from the apparent density of the powder (ρ_{app}):

$$g = 1 - \frac{\rho_{app}}{\rho_{sol}}$$

Combustion of Carbon in Casting Powder in a Temperature Gradient, Supradist *et al,* ISIJ International, 2004 [5]



Calculating effective powder thermal conductivities: Values

Property	1		Value	
<i>k_{sol}</i> (solid slag thermal conductivity)			2 W/m K	1.6 ▲ ■ measurement
k_{gas} is the the conductivity of t (Air)	ermal he gas	2.624 x	10 ⁻² W/m K	as received
$ ho_{sol}$ (Slag der	nsity)	2	600 kg/m ³	
$ \rho_{app} $ (Apparent of	density)	800 I 1400	kg/m ³ (300 K) kg/m ³ (1273 K)	0.4 - with 5 mass % graphite
Variable		Calculated Value		0 200 400 600 800 1000 temperature T, °C
Temperature	30	0 K	1273 K	Fig. A1. Apparent density of as-received casting powder and casting powder with 5 mass% graphite, as a function of tomographics.
g	0.	70	0.48	temperature.
k _{eff}	0.48 \	N/m K	0.90 W/m K	
Combustion of Ca International, 2004 H. W. Russel: <i>J. A</i>	arbon in C 4 [5] A <i>m. Cerar</i>	asting Po n. Soc., 1	wder in a Tempera 8 (1935) [6]	ture Gradient, Supradist <i>et al,</i> ISIJ
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Slag Thermal conductivity variation with Temperature

- The powder thermal conductivity is 0.5 W/m K at 300 K and increases linearly to 0.8 W/m K at 1173 K.
- The liquid slag thermal conductivity is taken to be 3 W/m K.

Slag / sintered layer temperature used to define liquid slag thickness is 1173 K (900 °C)



Transient Thermo-Fluid Model of Meniscus Behavior and Slag Consumption in Steel Continuous Casting, Jonayat *et al*, Metallurgical and Materials Transactions B, 2014 [7] McDavid & Thomas, Met Trans, 1996, 27(4) 672-685 [2] University of Illinois at Urbana-Champaign





Calculation of Downward Velocity in the Flux Layer: Equations

• The negative strip time is calculated using:

$$t_n = \frac{1}{\pi f(\frac{cycles}{s})} \cos^{-1}(\frac{v_s(\frac{mm}{s})}{\pi s (mm) f(\frac{cycles}{s})})$$
$$t_p = T - t_n$$

- Where f = oscillation frequency, s = stroke of oscillation, T = total cycle time
- Total flux consumption per cycle (g/m cycle)= $q_C = q_{OM} + q_{lub}$
- Total Flux consumption per second per unit length (g/m s) = $q_S = q_C \times f$
- Total flux consumption (g/s) = q_{t_T} = q_S x slab perimeter = q_S x 2(slab thickness + slab width) = q_S x 2 (t + w)
- Velocity (mm/s) = $\frac{q_{t_T}}{Slab Area \times \rho_{slag}}$
- Total Powder Flux consumption per unit area (kg/m²) = Q = $q_C \frac{f}{v_c}$

AIST Continuous Casting: A Practical Training Seminar, Brian G. Thomas, Indianapolis, IN, Oct 2014 [9]

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Parameters used for flux consumption determination

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Parameter	Value
$ ho_{slag}$ (Density of slag)	2600 kg /m ³
$\Delta ho~$ (Density difference between slag and steel)	4527 kg/m ³
Vs (Casting Speed)	27.5 mm/s
k (Empirical Constant depends on powder composition)	12
Δγ	1.3 N/m
Frequency of mold oscillation	2.9 Hz
Stroke of oscillation	6 mm
Slab Thickness	0.203 m
Slab Width	1.7 m
Positive Strip Time	0.23 s
Negative Strip Time	0.11 s

Measurement and Prediction of Lubrication, Powder Consumption, and Oscillation Mark Profiles in Ultra-low Carbon Steel Slabs, Shin *et al*, ISIJ International, 2006 [8] Nailboard Measurements of Surface Flow at Severstal, Mihir Chavan CCC Annual Report 2013 [3]



Assumptions used in considering consumption parameter values

- The Casting speed, slab thickness and slab width values were obtained from the experiment conducted at Severstal.
- The frequency and stroke of the mold oscillation values were taken from the work of Shin *et al.*
- The value for the empirical constant was assumed to be equal to 12. The value of the empirical constant depends on the powder composition. (Note: The empirical constants depending on the powder properties used by Shin *et al* are 15.8 for Group A flux and 14 for Group C flux)

II. Mold Powder (Trial A and B):		III. Mold Powder (Trial C):		
$CaO\left(39.8\% \right) - SiO_{2}\left(36.3\% \right) - Al_{2}O_{3}\left(3.4\% \right) - MgO\left(0.8\% \right) - Li_{2}O\left(0.4\% \right) - Na_{2}O\left(3.4\% \right) - MgO\left($		$CaO~(37.9\%) - SiO_2~(37.8\%) - Al_2O_3~(5.0\%) - MgO~(2.0\%) - Li_2O~(0.9\%) - Na_2O~(3.8\%) - MgO~(3.8\%) - MgO~(3.$		
$\mathbf{K_{2}O}\;(0.1\%)-\mathbf{Fe_{2}O_{3}}\;(0.3\%)-\mathbf{MnO_{2}}\;(0.03\%)-$	$TiO_2(0.2\%) - F(6.0\%) - CO_2(3.5\%) - C_{total}(3.0\%)$	$\mathbf{K_{2}O}\;(0.1\%)-\mathbf{Fe_{2}O_{3}}\;(0.3\%)-\mathbf{MnO_{2}}\;(0.04\%)-$	$TiO_2(0.3\%) - F(7.2\%) - CO_2(3.2\%) - C_{total}(2.6\%)$	
Density of liquid slag (kg m ⁻³)	2680	Density of liquid slag (kg m ⁻³)	2660	
Viscosity at 1300 °C (Pa s)	0.321	Viscosity at 1300 °C (Pa s)	0.262	
Surface tension (N m ⁻¹)	0.431	Surface tension (N m ⁻¹)	0.419	
Solidification temperature (°C)	1145	Solidification temperature (°C)	1101	
Melting temperature (°C)	1180	Melting temperature (°C)	1145	

• The empirical constant value of 12 indicates a lower melting temperature for the slag chosen.

Measurement and Prediction of Lubrication, Powder Consumption, and Oscillation Mark Profiles in Ultra-low Carbon Steel Slabs, Shin *et al*, ISIJ International, 2006 [8] University of Illinois at Urbana-Champaign • Metals Processing Simulation Lab • Adnan Akhtar • 15



Flux Consumption and Axial Velocity Calculated

Parameter	Value Calculated
Oscillation Mark Consumption per cycle = q_{OM} (g/m cycle)	0.47 g/m cycle
Lubrication Consumption per cycle = q_{lub} (g/m cycle) (Includes both solid and liquid slag)	1.16 g/m cycle
Total Flux consumption per cycle = q_c	1.63 g/m cycle
Total Flux consumption per second per unit length = q_s	4.71 g/m s
Total flux consumption (g/s) = q_{t_T}	17.94 g/s
Total Powder Consumption per unit area = Q	0.171 kg/m ²
Axial Velocity of flux	0.020 mm/s



Calculation of Surface Heat transfer coefficient (Parameters considered)

Parameter	Value
Emissivity of Air	0.8
Ambient Temperature (Tamb)	300 K
Kinematic Viscosity of Air	$1.568 \times 10^{-5} \text{ m}^2/\text{s}$
Thermal conductivity of air	2.624 x 10 ⁻² W/m K
Specific heat of air	1004.9 J/kg K
Coefficient of Thermal Expansion for air	3.35 x 10 ⁻³ 1/K
Slab Width	1.7 m
Slab Thickness	0.203 m



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Correlations for Heat Transfer Coefficient Calculation

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- The correlation for calculation of heat transfer coefficient is based on natural convection over a rectangular plate of known dimensions (McAdam's correlation).
- The Convective Heat Transfer coefficient is calculated using the empirical relation:
 - $Nu = 0.14 \ Ra^{0.33}$ for $Ra = 2 \ge 10^7 3 \ge 10^{10}$

Where Ra is the Rayleigh number.

$$Ra = \frac{\rho g \beta \Delta T L^3}{\mu \alpha}$$

 Characteristic length = L = average of the slab width and slab thickness

$$h_{con} = Nu \; \frac{k_{air}}{L}$$

• The Heat Transfer coefficient for radiation is calculated using: $h_{rad} = \sigma \varepsilon (To^4 - Tamb^4)$

W.H. McAdams, Heat Transmission, 3rd ed, McGraw Hill, 1954 [10] Convective Heat Transfer, Louis C Burmeister (Pg 550) [11] 17









Increasing Flux Consumption with time

- The transient simulation is based on an increasing flux consumption (axial velocity) with time.
- Initially, there is only powder in the flux layer and no flux consumption. As the powder heats up, it melts to form the liquid slag layer. The growth of the liquid slag layer results in an increase in the flux consumption.
- Thus, the consumption increases from 0 to a steady value of 4.71 g/m s (0.02 mm/s). For this simulation, the consumption is increased in steps after every 120 s until it reaches the steady value after 960 s.



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Inferences from the transient behavior in the flux layer

• Initially the entire layer is composed of only powder flux. With increasing time the powder melts to form the sintered and the liquid flux layer. The liquid layer thickness increases until the heat from the molten steel equals the heat loss to the atmosphere.

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- The change in slope (kink) observed in the temperature plot is at the liquid slag-powder interfacial (Sintered) region. The slope change is due to high-thermal conductivity liquid slag dropping to low-conductivity powder.
- A higher consumption lowers the temperature in the slag greatly.
- The increasing consumption with time reaches steady state in a shorter time than with either the no consumption or constant consumption case.





Tempering Colors of Steel (Tool Steel Color vs Temperature)

Tool Steel Color vs Temperature

2000°E		
2000 F	Bright yellow	1093°C
1900°F	Dark yellow	1038°C
1800°F	Orange yellow	982°C
1700°F	Orange	927°C
1600°F	Orange red	871°C
1500°F	Bright red	816°C
1400°F	Red	760°C
1300°F	Medium red	7 0 4°C
1200°F	Dull red	649°C
1100°F	Slight red	593°C
1000°F	Very slight red, mostly grey	538°C
0800°F	Dark grey	427°C
0.77	71	
0575°F	Blue	302°C
0575°F 0540°F	Blue Dark Purple	302°C 282°C
0575°F 0540°F 0520°F	Blue Dark Purple Purple	302°C 282°C 271°C
0575°F 0540°F 0520°F 0500°F	Blue Dark Purple Purple Brown/Purple	302°C 282°C 271°C 260°C
0575°F 0540°F 0520°F 0500°F 0480°F	Blue Dark Purple Purple Brown/Purple Brown	302°C 282°C 271°C 260°C 249°C
0575°F 0540°F 0520°F 0500°F 0480°F 0465°F	Blue Dark Purple Purple Brown/Purple Brown Dark Straw	302°C 282°C 271°C 260°C 249°C 241°C
0575°F 0540°F 0520°F 0500°F 0480°F 0465°F 0445°F	Blue Dark Purple Purple Brown/Purple Brown Dark Straw Light Straw	302°C 282°C 271°C 260°C 249°C 241°C 229°C

- It is known that the diameter of the nail used for the experiment is 5 mm.
- Using this as scale, the distances along the length of the nail can be measured using a photograph of the nail.
- The steel-flux interface is at the mean distance between the top and bottom surface of the solidified steel.
- This is due to the fact that on dipping of the nail, a wave is generated. The higher region corresponds to the side towards which the molten steel is flowing.

threeplanes.net/toolsteel.html [12]





Calculation of Nail Dipping Time

- From the image, the thickness of the lump formed on the nail is found out to be 4.3 mm.
- The solidification time for the lump is found out using the following equation:

$$s = k \sqrt{t}$$

- *s* = lump thickness
- $k = 1.1 \operatorname{inch}/\sqrt{\min} = 3.6 \times 10^{-3} \mathrm{m}/\sqrt{s}$
- Solidification Time Calculated = 1.42 s
- A nail dipping time of 1.5 s was selected for the simulation. (Generally 1-3 s is the dipping time used by researchers)







Flux and Steel Properties used in the simulation

- Slag Density = 2600 kg/m³
- Steel Density= 8030 kg/m³
- Steel Specific Heat = 502.5 J/kg K
- Steel Thermal Conductivity = 16.3 W/m K



Slag Thermal Conductivity k = 0.5 W/m K at T = 300 K Linearly increases to 0.8 W/m K 300 K < T < 1173 K Linearly increases to 3 W/m K at 1273 K 1173 K < T < 1273 K k = 3 W/m K, T> 1273 K



http://www.arc.vt.edu/ansys_help/flu_ug/flu_ug_biblio.html#XUGhsu-jemcov [13]











Parametric Study using a steel nail (Effect of Nail Dipping Time)

Effect of Nail Dipping Time

Flux consumption = 4.71 g/m s (0.02 mm/s velocity), Total Slag Thickness = 50 mm

Nail Dipping Time (s)	Liquid Flux Layer Thickness (mm)	Distance of discoloration (555 K) from lump (mm)	% Liquid Flux Layer / Distance of discoloration from lump
1 s	19.0 mm	19.5 mm	97.4 %
1.5 s	19.0 mm	21.0 mm	90.5 %
3 s	19.0 mm	24.5 mm	77.5 %
4 s	19.0 mm	26.0 mm	73.0 %
5 s	19.0 mm	27.5 mm	69.0 %
6 s	19.0 mm	28.5 mm	66.7 %

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Parametric Study using a steel nail (Effect of Total Flux Layer Thickness)

Effect of Total Flux Layer Thickness

Flux consumption constant = 4.71 g/m s (0.02 mm/s velocity), Nail Dipping Time = 1.5 s

Total Flux Layer Thickness (mm)	Liquid Flux Layer Thickness (mm)	Distance of discoloration (555 K) from lump (mm)	% Liquid Flux Layer / Distance of discoloration from lump
30 mm	19.0 mm	21.0 mm	90.5 %
40 mm	19.5 mm	21.8 mm	89.5 %
50 mm	19.0 mm	21.0 mm	90.5 %

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Parametric Study using a steel nail (Effect of Flux Consumption and dipping time)

Effect of Flux Consumption Total Flux Layer Thickness = 50 mm, Nail Dipping Time = 1.5 s				
Flux Consumption (g/m s)	Liquid Flux Layer Thickness (mm)	Distance of discoloration (555 K) from lump (mm)	% Liquid Flux Layer / Distance of discoloration from lump	
3.41 g/m s	26.0 mm	29.4 mm	88.4 %	
4.71 g/m s	19.0 mm	21.0 mm	90.5 %	
7.06 g/m s	11.9 mm	13.6 mm	87.5 %	
Total Flux Layer Thickness = 50 mm, Nail Dipping Time = 3 s				
Flux Consumption	Liquid Flux Layer Thickness (mm)	Distance of discoloration	% Liquid Flux Layer / Distance of discoloration	
(g/m s)		(555 K) from lump (mm)	from lump	
(g/m s) 3.41 g/m s	26.0 mm	(555 K) from lump (mm) 33.3 mm	from lump 78.0 %	
(g/m s) 3.41 g/m s 4.71 g/m s	26.0 mm 19.0 mm	(555 K) from lump (mm) 33.3 mm 24.5 mm	from lump 78.0 % 77.5 %	
(g/m s) 3.41 g/m s 4.71 g/m s 7.06 g/m s	26.0 mm 19.0 mm 11.9 mm	(555 K) from lump (mm) 33.3 mm 24.5 mm 15.9 mm	from lump 78.0 % 77.5 % 74.8 %	



Inferences from the heat transfer in a steel nail

- Average Flux consumption of the three simulations is 5.06 g/m s. The local flux consumptions average out to give approximately the total flux consumption for the process.
- Regions near the SEN have lower consumption as compared to those near the narrow face. A larger consumption is observed for a smaller total flux layer thickness.
- The discoloration temperature from the experiment match with the simulation temperature for a dipping time of 1.5 s.
- The average nail temperature at the liquid layer thickness is 340 °C. (From the tempering colors of steel, this corresponds to a transition from dark grey to blue)
- Given the uncertainty of reading dark grey, it would be more accurate to measure from the dark purple discolored band (555 K) to the lump, and adjust according to:
 - Nail Dipping Time (90 % for 1.5 s and 75 % for 3 s)
- The flux consumption and total slag layer thickness do not have a significant effect on the % Liquid flux layer thickness to distance of discoloration from lump ratio.





- 1. The Aluminum Nail remains solid (300 933 K) until the Al melts.
- After the AI melts, the surrounding slag may solidify (933 1173 K) until the slag melts. There could be mixture of AI and slag in the column of molten material beneath the nail.
- 3. Above 1173 K, the powder melts to form the liquid slag. Therefore, molten Aluminum and liquid slag will co-exist above this temperature.
- 4. For analyzing this phenomenon, three cases are simulated:
 - Case 1: Solid Aluminum properties up to the melting temperature of Aluminum 933 K (660 °C). Molten Aluminum properties up to 1173 K (900 °C). Above 1173 K, slag properties.
 - Case 2: Scenario 1 dipped only in flux layer with 5mm liquid slag gap
 - Case 3: Dipped only in flux layer with 5mm liquid slag gap Solid Aluminum properties up to the melting temperature of Aluminum 933 K (660 °C). Slag properties up to 1173 K (900 °C). Above 1173 K, molten Aluminum properties.

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Properties defined in the nail region

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- The properties in the nail region in contact with the flux layer is defined by solid Aluminum properties up to the melting temperature of Aluminum 933 K (660 °C).
- 2. On melting the properties of molten Aluminum are considered until the slag melting temperature of 1173 K (900 °C).
- 3. Above 1173 K, slag properties are considered in the nail region.
- 4. Density in the region is constant = 2719 kg/m^3







Contours at 933 K and 1173 K indicates the melting temperature of Aluminum and slag respectively. University of Illinois at Urbana-Champaign • Metals Processing Simulation Lab • Adnan Akhtar •





Aluminum Nail Surface Temperature variation with time (Case 2: Nail dipped 35 mm into flux)

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- The approximate time for nail dipping remains the same for a nail dipped in molten steel and only dipped in the flux layer (6 s). (Case 1 and 2)
- The time required to match the liquid flux layer thickness increases to 30 s. (Case 3)
- The drop in temperature is greater for the slag as compared to the molten aluminum due to the low thermal conductivity of the slag as compared to aluminum.
- Aluminum nail may be an accurate method to determine the liquid flux layer thickness, but might be unreliable.

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Heat Transfer with slag consumption in the Flux Layer and Copper Nail

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Copper Properties used in the simulation

- Copper Density= 8940 kg/m³
- Copper Specific Heat = 390 J/kg K
- Copper Thermal Conductivity = 400 W/m K
- Molten Copper Specific Heat = 531.5 J/kg K
- Molten Copper Thermal Conductivity = 160 W/m K
- Melting Temperature of Copper = 1358 K

http://www.arc.vt.edu/ansys_help/flu_ug/flu_ug_biblio.html#XUGhsu-jemcov [13] http://www.engineeringtoolbox.com/ [14] Thermal conductivity measurement of molten copper using an electromagnetic levitator superimposed with a static magnetic field, Baba *et al*, Measurement Science and Technology 2012 [15]

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Physical Significance of the properties in the nail region for a Copper nail

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- 1. The Copper Nail remains solid until the temperature is lower than its melting temperature of 1358 K (1058 °C) .
- 2. As the Copper melts it forms molten copper. At this temperature, the slag is also in the liquid state.
- 3. As a result, at a temperature greater than 1358 K molten copper and liquid slag co-exist in the flux layer.
- 4. Two scenarios have been simulated for the copper nail:
 - Solid Copper at temperatures below 1358 K and liquid slag above 1358 K.
 - Solid Copper at temperatures below 1358 K and molten Copper above 1358 K.





Conclusions (Copper Nail)

- Dipping a copper nail into the flux layer with a 5-mm gap above the molten steel: did not melt if the gap fills with liquid slag.
- Dipping a copper nail into the molten steel:
 - If the melted copper region stays filled with liquid copper, the nail eventually melts back to match the liquid slag layer thickness (7% error) after 80s.
 - If the melted copper is replaced with liquid slag, only 5-mm liquidslag gap forms.
 - Thus, using copper nail is not reasonable (melting temp is too high).
 - Even using copper wire may not be reliable



- Dipping an Aluminum nail into the molten steel (Case 1)
 - If melted AI is initially a continuous column and later its bottom is replaced by slag, it takes 6 s to match the liquid flux layer thickness.
- Dipping an Aluminum nail into the flux layer (Case 2 & 3)
 - It still takes 6 s to match the liquid flux layer thickness (Similar to Case 1).
 - If the top of the column sinks beneath a solid slag barrier (Case 3), it takes 30 s to match the liquid flux layer thickness.
- Same amount of time to predict liquid flux layer thickness for a nail dipped in molten steel and flux only.
- In 3 seconds, the predicted value reaches within 20 % of the actual liquid flux layer thickness. (Case 1 and 2)
- Aluminum nail may be an accurate method to determine the liquid flux layer thickness, but might be unreliable.

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Conclusions (Steel Nail) and Future Work

- For a steel nail, the average nail temperature was 340 °C at the location of the liquid flux layer thickness falls between dark grey and blue tempering colors of steel oxide (125 °C range).
- This suggests that the gray-blue tempering color on the steel nail can approximate the liquid-slag layer depth.
- Given the uncertainty of reading dark grey, it would be more accurate to measure from the dark purple discolored band (555 K) to the lump, and adjust according to:
 - Dipping time (90% at 1.5 s to 75% at 3 s)
- The flux consumption and total slag layer thickness do not significantly change this percentage.
- The aluminum nail dipped for 6s might give a better prediction, but depends on the melting / property scenario.
- Future Work: Validate this methodology to predict liquid flux layer thickness with plant experiments.

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References

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- 1) Dauby et al, LTV Steel, 1985; SM-Cho et al, TMS, 2011
- 2) McDavid & Thomas, Met Trans, 1996, 27(4) 672-685
- 3) Nailboard Measurements of Surface Flow at Severstal, Mihir Chavan CCC Annual Report 2013
- 4) Experiments conducted by Liu et al, Oct. 14-15, 2012 at Severstal
- 5) Combustion of Carbon in Casting Powder in a Temperature Gradient, Supradist *et al,* ISIJ International, 2004
- 6) H. W. Russel: J. Am. Ceram. Soc., 18 (1935)
- 7) Transient Thermo-Fluid Model of Meniscus Behavior and Slag Consumption in Steel Continuous Casting, Jonayat and Brian G. Thomas, Metallurgical and Materials Transactions B, 2014
- 8) Measurement and Prediction of Lubrication, Powder Consumption, and Oscillation Mark Profiles in Ultra-low Carbon Steel Slabs, Shin *et al*, ISIJ International, 2006
- 9) AIST Continuous Casting: A Practical Training Seminar, Brian G. Thomas, Indianapolis, IN, Oct 2014
- 10) W.H. McAdams, Heat Transmission, 3rd ed, McGraw Hill, 1954
- 11) Convective Heat Transfer, Louis C Burmeister, P550
- 12) threeplanes.net/toolsteel.html
- 13) http://www.arc.vt.edu/ansys_help/flu_ug/flu_ug_biblio.html#XUGhsu-jemcov
- 14) http://www.engineeringtoolbox.com/
- 15) Thermal conductivity measurement of molten copper using an electromagnetic levitator superimposed with a static magnetic field, Baba *et al*, Measurement Science and Technology 2012

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